

COMPITO ELETTROTECNICA 10-12-2014

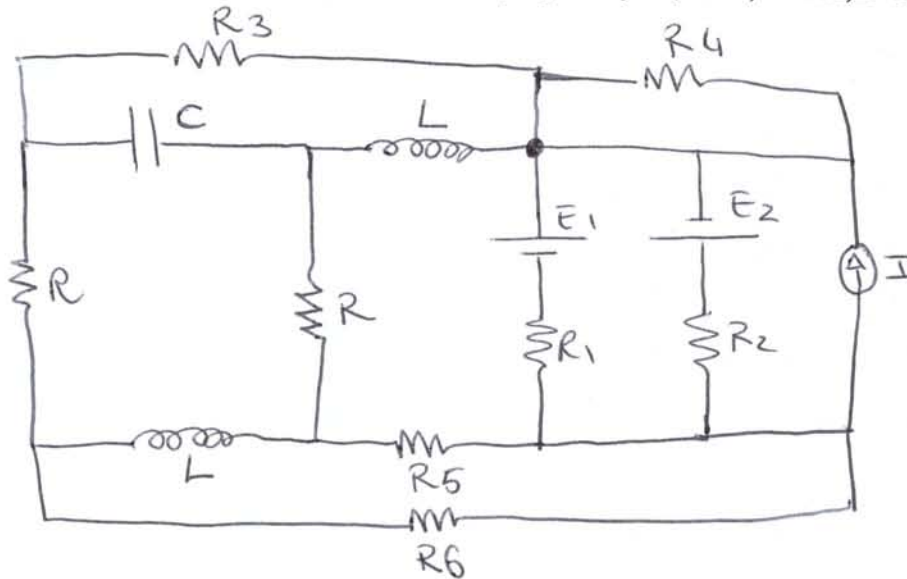
Allievo _____ Matricola: _____

Corso di Laurea: _____

Esercizio 1:

Il circuito in figura è a regime. Determinare le potenze generate ed erogate da E_1 - R_1 ed E_2 - R_2 .

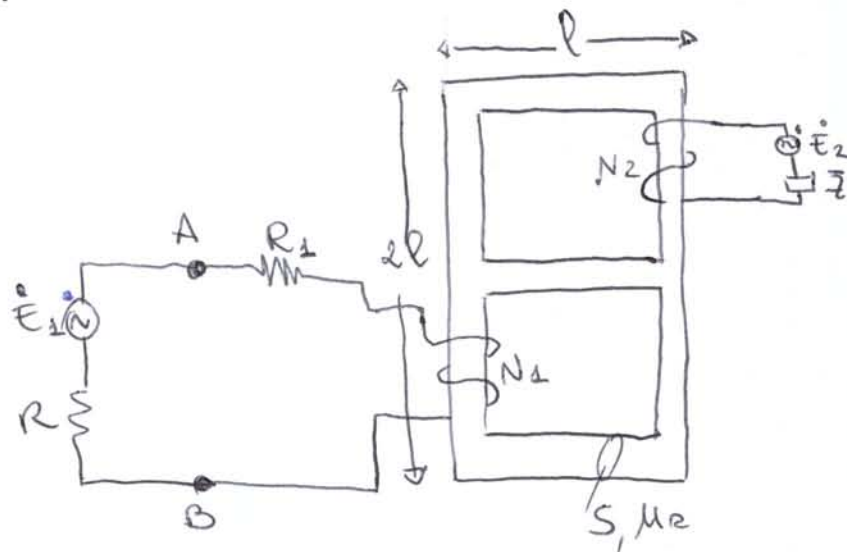
$E_1 = 5V$; $E_2 = 7V$; $R = 1\Omega$; $R_1 = R_5 = R_6 = 5\Omega$; $R_2 = 3\Omega$; $R_3 = 3\Omega$; $R_4 = 4\Omega$; $I = 2A$; $L = 3mH$; $C = 3mF$.



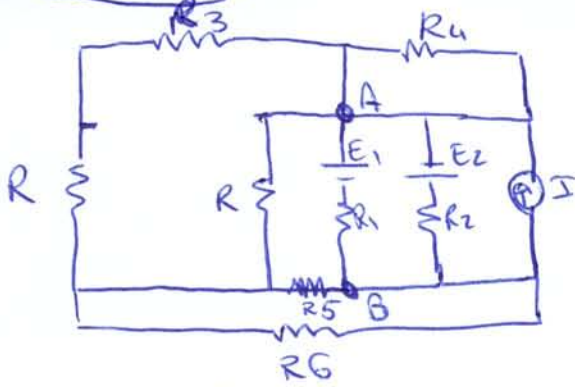
Esercizio 2:

Dato il seguente circuito a regime, determinare la capacità da inserire tra i punti A e B, per rifasare il sistema a $\cos \Phi = 0.9$.

$\dot{E}_1 = 5V$; $\dot{E}_2 = 7V$; $\bar{Z} = 3 + j \Omega$; $R = 5 \Omega$; $R_1 = 3 \Omega$; $N_1 = 200$; $N_2 = 250$; $\omega = 10 \text{ rad/sec}$; $l = 2 \text{ cm}$, $S = 1,5 \text{ cm}^2$; $\mu_r = 1000$.



ES. N° 1

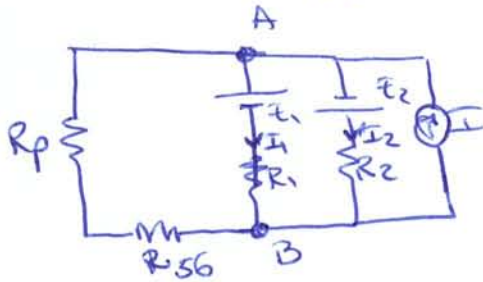


R_4 trascurabile in quanto in // a

$$R_{56} = R_5 // R_6$$

$$R_{\Delta} = R + R_3$$

$$R_0 = R_5 // R_6$$



=>



$$E_M = \frac{E_1}{R_1} - \frac{E_2}{R_2} + I$$

$$\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_p + R_5}$$

$$V_{AB} = E_M$$

$$V_{AB} - E_1 = I_1 \cdot R_1 \Rightarrow I_1 = \frac{V_{AB} - E_1}{R_1}$$

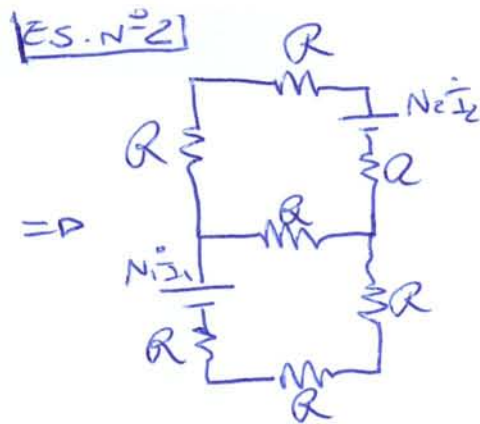
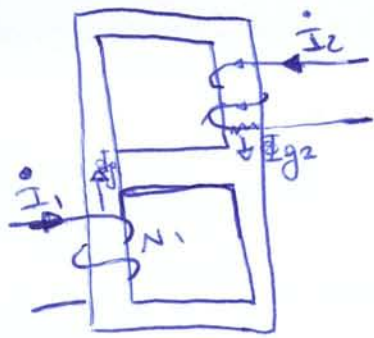
$$V_{AB} + E_2 = I_2 \cdot R_2 \Rightarrow I_2 = \frac{V_{AB} + E_2}{R_2}$$

$$P_{g_{E_1-R_1}} = E_1 \cdot (-I_1)$$

$$P_{e_{E_1-R_1}} = V_{AB} \cdot (-I_1)$$

$$P_{g_{E_2-R_2}} = E_2 \cdot (I_2)$$

$$P_{e_{E_2-R_2}} = V_{AB} \cdot I_2$$



$$R = \frac{l}{\mu_0 \mu_r S} = 1.06 \cdot 10^5 \Omega$$

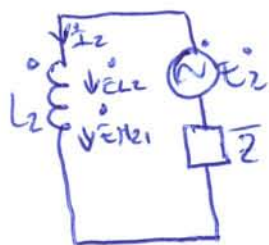
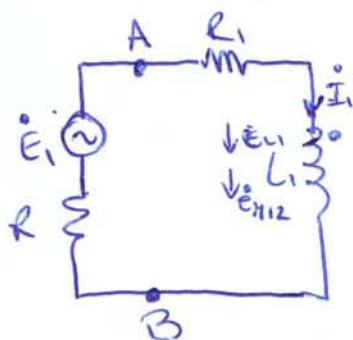
$$R_{eq1} = (3R \parallel R) + 3R = 4R$$

$$R_{eq2} = (3R \parallel R) + 3R = 4R$$

$$R_{eq} = R_{eq1} = R_{eq2} = 4 \cdot 10^5 \Omega$$

$$L_1 = \frac{N_1^2}{R_{eq}} = 0.14 \text{ H}; \quad M_{12} = \frac{N_1 N_2}{R_{eq}} \alpha_{12} = \frac{N_1 N_2}{\frac{15}{4} R} \cdot \frac{R}{3R+R} = \frac{N_1 N_2}{15R} = 0.03 \text{ H}$$

$$L_2 = \frac{N_2^2}{R_{eq}} = 0.14 \text{ H} \quad M_{12} = M_{21} (> 0)$$



$$\begin{cases} \dot{E}_1 + \dot{E}_{L1} + \dot{E}_{M12} = \dot{I}_1 (R + R_1) \\ \dot{E}_2 + \dot{E}_{L2} + \dot{E}_{M21} = \dot{I}_2 Z \end{cases}$$

$$\begin{cases} \dot{E}_1 - j\omega L_1 \dot{I}_1 - j\omega M_{12} \dot{I}_2 = \dot{I}_1 (R + R_1) \\ \dot{E}_2 - j\omega L_2 \dot{I}_2 - j\omega M_{21} \dot{I}_1 = \dot{I}_2 Z \end{cases}$$

$$\Rightarrow \begin{cases} \dot{I}_1 \\ \dot{I}_2 \end{cases} = \begin{pmatrix} 0,57 + j0,11 \\ 1,04 - j1,2 \end{pmatrix} \text{ A}$$

$$\bar{S}_{AB} = \dot{V}_{AB} \cdot \dot{I}_1^* = (\dot{E}_1 \cdot \dot{I}_1, R) \cdot \dot{I}_1^* = P_{CA} + jQ_{CA}$$

$$C = \frac{Q_{CA} - P_{CA} \tan \varphi}{\omega \cdot |\dot{V}_{AB}|^2}$$

$$\bar{S}_{AB} = \dot{V}_{AB} \cdot \dot{I}_1^* = (2,15 + j0,55) \cdot (0,57 + j0,11)^* = (1,16 + j0,55) \text{ VA}$$

$$\varphi_{CA} = \arctan \frac{0,55}{1,16} = 25,36^\circ \Rightarrow \cos \varphi_{CA} = 0,903 > \cos \varphi_R$$

Non si deve aphasare in quanto si è ottenuto un $\cos \varphi_{CA} > \cos \varphi_R$ ovvero si è ottenuto un fattore di potenza maggiore di quello richiesto.